### Section 5.5: DIVIDING POLYNOMIALS

When you are done with your homework you should be able to...

- $\pi$  Use the quotient rule for exponents
- $\pi$  Use the zero-exponent rule for exponents
- $\pi$  Use the quotients-to-power rule
- $\pi$  Divide monomials
- $\pi$  Check polynomial division
- $\pi$  Divide a polynomial by a monomial

### WARM-UP:

1. Find the missing exponent, designated by the question mark, in the final step:

$$\frac{x^8}{x^3} = \frac{\cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x}}{\cancel{x} \cdot \cancel{x} \cdot \cancel{x}} = x^?$$

2. Simplify:

$$\frac{\left(2a^3\right)^5}{\left(b^4\right)^5}$$

## THE QUOTIENT RULE FOR EXPONENTS

When dividing \_\_\_\_\_\_ expressions with the \_\_\_\_\_ nonzero base, \_\_\_\_\_ the exponent in the \_\_\_\_\_ from the \_\_\_\_\_ in the \_\_\_\_\_ of the \_\_\_\_\_ of the \_\_\_\_ base.

Example 1: Simplify each expression.

a. 
$$\frac{2^5}{2^3}$$

b. 
$$\frac{x^{10}}{x^8}$$

# THE ZERO-EXPONENT RULE

If \_\_\_\_\_ is any \_\_\_\_\_ number other than \_\_\_\_\_,

Example 2: Simplify each expression.

a. 
$$(4^2)^0$$

b.  $-7x^0$ 

## THE QUOTIENTS-TO-POWERS RULE FOR EXPONENTS

If \_\_\_\_ and \_\_\_ are real numbers and \_\_\_ is nonzero, then

When a \_\_\_\_ is \_\_\_\_ to a \_\_\_\_, \_\_\_\_

the \_\_\_\_\_ to the \_\_\_\_ and \_\_\_\_ by the \_\_\_\_\_ raised to the \_\_\_\_\_.

Example 3: Simplify each expression.

a. 
$$\left(\frac{x}{3}\right)^5$$

b. 
$$\left(\frac{4x^3}{5y}\right)^2$$

### DIVIDING MONOMIALS

To \_\_\_\_\_\_, \_\_\_\_the \_\_\_\_\_ and then divide the \_\_\_\_\_.

Use the \_\_\_\_\_ rule for \_\_\_\_\_ to divide the \_\_\_\_\_.

Example 4: Divide.

a. 
$$\frac{16x^4}{2x^4}$$

b. 
$$\frac{6x^2y^5}{21xy^3}$$

c. 
$$\frac{35r^8}{14r^7}$$

# DIVIDING A POLYNOMIAL THAT IS NOT A MONOMIAL BY A MONOMIAL

To \_\_\_\_\_\_ by a \_\_\_\_\_\_, \_\_\_\_each \_\_\_\_ of the \_\_\_\_\_ by the \_\_\_\_\_.

Example 5: Find the quotient.

a. 
$$(24x^6 - 12x^4 + 8x^3) \div (4x^3)$$

b. 
$$\frac{459x^{10}y^9 + 18x^5y^3 - 9x^4y}{-9x^3y}$$